References for Today’s Lecture

● Required reading
  – Section 18.8

● References
  – AMO Sections 3.4
  – CLRS Chapter 22
General Graph Search

- Depth-first search is so called because the node selected in each step is a neighbor of the node that is farthest from the root (in the tree).
- This is convenient because it allows a simple recursive implementation.
- Could we search the graph in a different “order”? 
**General Search Algorithm**

This is what a more general search algorithm might look like.

**Input:** Graph $G = (N, A)$ and source node $s \in N$

1. $Q \leftarrow \{s\}$
2. while $Q \neq \emptyset$ do
3. remove the “next” node $v$ from $Q$
4. mark $v$
5. process $v$
6. for $w \in A(v)$ do
7. process $(v, w)$
8. if $w$ is not marked then
9. $Q \leftarrow Q \cup \{w\}$
10. end if
11. end for
12. end while

(Figure 9.1 from Papadimitriou and Steiglitz)
Search Algorithm

• The search proceeds differently depending on which element $v$ is selected from $Q$ on line 3 in each iteration.

• $Q$ must be ordered in some way by storing it in an appropriate data structure.
  – If $Q$ is a queue, elements are inserted at one end and removed from the other and we get FIFO ordering.
  – If $Q$ is a stack, elements are inserted and deleted from the same end and we get LIFO ordering.

• The efficiency of the algorithm can be affected by
  – the data structure used to maintain $Q$,
  – what additional steps are required in processing $v$ (line 5),
  – what additional steps are required in processing $(v, w)$ (line 7).
Complexity of Search Algorithms

1. Initialization.

2. Maintaining the set $Q$.
   - What is the maximum number of additions and removals?
   - How many operations are required for each?

3. Searching the adjacency lists.
   - How many times do we touch each element of each list?
   - How much work do we do each time we touch an element?

4. Processing a node.


Algorithm Search

• The algorithm is a template for a whole class of algorithms.
  – If $Q$ is a *stack* (LIFO), we are doing something like depth-first search, as before (but not precisely...).
  – If $Q$ is a *queue* (FIFO), we are doing *breadth-first search*.
  – In other cases, we will want to maintain $Q$ as a priority queue.

• What problem does breadth-first search of a graph solve?